

Kinetics & Reactor Design 2: Liquid Reactors

CSTR Des 1

Continuing Ed workshop by Richard Skeirik, PE

CSTR Design Exercise

The reaction is a simple irreversible isomerization: $A \rightarrow B$

The reaction rate is $r_a = -k_f A$. $k_f = 5 \text{ min}^{-1}$

An upstream unit dictates a feed concentration of 2.5 mol/m^3

The business leaders have given us a design objective for a reactor to create 8 mol/min of B

The CSTR balance (you derived this, remember?) is

$$qA_{in} - qA_{out} - Vk_f A_{out} = 0$$

Approach 1: Set Conversion

Name	Value	Units
Kf	5	min^{-1}
q		m^3/min
Ain	2.5	mol/m^3
Aout		mol/m^3
q•Bout	8.0	mol/min
V		m^3

Here is an insight that makes this problem easier. Since A simply goes to B, you form one mole of B for each mol of A that reacts. So the amount of B exiting (your design variable) is simply equal to the amount of A reacting. Now, which term in the balance is that? Write this equivalence:

$$[\text{design spec}] = [\text{amount of a reacting}]$$

We are already close to being finished. Only V and Aout are unknown. One equation, two unknowns. The choice is ours as designer, so let's **set a conversion** of A. Let's say 80% of A is reacted.

$$A_{out} = 0.2 \cdot A_{in}$$

Compute that and put it in the table. Now we have one equation to give V. What is V?

This is your reactor design

80% conversion

$$V = \text{_____} \text{ m}^3$$

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What is q ?

$$q [A_{in} - A_{out}] = V k_f A_{out} = 8 \text{ mol/min.}$$

Add that to your table.

Approach 2: Set V

What if you already have a 5 m^3 reactor? Let's run at the same q , A_{in} as above.

Name	Value	Units
K_f	5	min^{-1}
q	4.0	m^3/min
A_{in}	2.5	mol/m^3
A_{out}		mol/m^3
$q \bullet A_{out}$	8.0	mol/min
V	5	m^3

$$q A_{in} - q A_{out} - V k_f A_{out} = 0$$

Again, the production spec is the rate of reaction of A:
[amount of A reacting] = [design spec of 8 mol/min]

One equation, one unknown. Solve for A_{out} . Put it in your table

High Conversion

Let's go back to the first case. Instead of 80% conversion, let's design for 99.99% conversion. What reactor volume do you need?

Why is the reactor so big?